

Remark 0.0.1. Doob's measurability theorem tells us for an integrable random variable Y , $\mathbb{E}[Y|\sigma(X)]$ which by definition is $\sigma(X)$ -measurable, must be a function of X .