

Definition 0.0.1 (Ito's integral for general integrands). For any process $\gamma \in L^2_{\mathbb{P}}(W)$, the random variable $I_T(\gamma)$ is called Ito's integral of γ with respect to W over $[0, T]$. We write (notation only, not a formal definition):

$$I_T(\gamma) = \int_0^T \gamma_u \cdot dW_u$$

$$I_t(\gamma) = I_T(\gamma \mathbf{1}_{[0,t]}) = \int_0^t \gamma_u \cdot dW_u$$