

**Proposition 0.0.1.** Suppose that  $\gamma$  is an  $\mathbb{R}^d$ -valued  $\mathcal{F}$ -progressively measurable process such that  $\mathbb{E}^{\mathbb{P}}[\mathcal{E}_T(U)] = 1$ . Define a probability measure  $\tilde{\mathbb{P}}$  on  $(\Omega, \mathcal{F}_T)$  equivalent to  $\mathbb{P}$  by means of the Radon–Nikodym derivative

$$\eta_T = \frac{d\tilde{\mathbb{P}}}{d\mathbb{P}} = \mathcal{E}_T \left( \int_0^T \gamma_u \cdot d\mathbf{W}_u \right) = \mathcal{E}_T(U).$$

Then the process  $\tilde{\mathbf{W}}$  given by the formula

$$\tilde{\mathbf{W}}_t = \mathbf{W}_t - \int_0^t \gamma_u \, du, \quad \forall t \in [0, T]$$

follows a standard  $d$ -dimensional Brownian motion on the space  $(\Omega, \mathcal{F}, \tilde{\mathbb{P}})$ .