

**Definition 0.0.1** (almost sure equality of two r.v.s). Two random variables  $X$  and  $Y$  are said to be **equal almost surely**, written  $X \stackrel{\text{a.s.}}{=} Y$  if the set  $\{\omega : X(\omega) \neq Y(\omega)\}$  is of probability zero.